

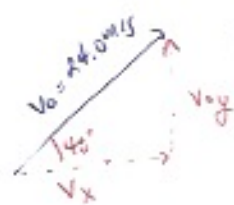
**Physics: Kinematics in Two-Dimensions**  
**Class Examples**

**Full Projectile:**

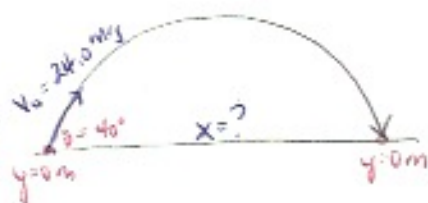
**Example 2:**

The Human Cannonball in the Ringling Bros. and Barnum & Bailey Circus, was fired out of a cannon with an initial velocity ( $v_0$ ) of 24.0 m/s at an angle of  $40.0^\circ$  with respect to the ground.

- Find the x- and y-components of the initial velocity
- After the cannon firing, how long was he in the air?
- With the initial velocity described above, where would the safety net need to be placed in order to catch him at the end of his flight?



A)  $v_x = \cos(40.0^\circ) \cdot 24.0$   
 $v_x = 18.4 \text{ m/s}$   
 $v_y = \sin(40.0^\circ) \cdot 24.0$   
 $v_y = 15.4 \text{ m/s}$



C)  $x = v_x \cdot t$   
 $x = (18.4)(3.14)$   
 $x = 57.8 \text{ m}$

$x =$   
 $v_x = 18.4 \text{ m/s}$   
 $t = 3.14 \text{ s}$

$y =$   
 $y = 0 \text{ m (start + end)}$   
 $v_{y0} = 15.4 \text{ m/s}$   
 $v_y =$   
 $a_y = -9.8 \text{ m/s}^2$   
 $t = 3.14 \text{ s}$

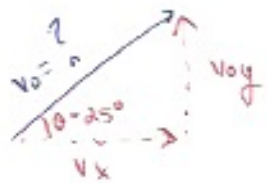
B)  $t = ?$   
 $y = 0 \text{ m}$   
 $v_{y0} = 15.4 \text{ m/s}$   
 $a_y = -9.8 \text{ m/s}^2$

$y = v_{y0}t + \frac{1}{2}a_y t^2$   
 $0 = 15.4t + \frac{1}{2}(-9.8)t^2$   
 $0 = (15.4 - 4.9t)t$   
 $15.4 - 4.9t = 0$   
 $-4.9t = -15.4$   
 $t = \frac{-15.4}{-4.9}$   
 $t = 3.14 \text{ s}$

**Example 3:**

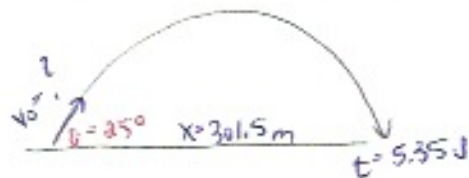
A golfer hits a golf ball, giving the ball an initial velocity ( $v_0$ ) at an angle of  $25.0^\circ$ . The ball flies through the air for 5.35 s before landing a horizontal distance of 301.5 m away from the tee.

- What was the initial velocity ( $v_0$ )?
- What is the maximum height the ball reaches?



$v_x = \cos(25^\circ) \cdot v_0$

$v_y = \sin(25^\circ) \cdot v_0$



A)  $v_0 = ?$   
 we can use either  
 $v_x = \cos(25^\circ) \cdot v_0$   
 or  
 $v_y = \sin(25^\circ) \cdot v_0$

Now use  $v_x = 56.4 \text{ m/s}$  here

$v_x = \cos(25^\circ) \cdot v_0$   
 $56.4 = \cos(25^\circ) \cdot v_0$   
 $v_0 = \frac{56.4}{\cos(25^\circ)}$

Find  $v_x$  first

$x = v_x \cdot t$   
 $301.5 = v_x \cdot 5.35$   
 $v_x = \frac{301.5}{5.35}$   
 $v_x = 56.4 \text{ m/s}$

$v_0 = 62.2 \text{ m/s}$

$x =$   
 $x = 301.5 \text{ m}$   
 $v_x =$   
 $t = 5.35 \text{ s}$   
 $y =$   
 $y = 0 \text{ m (start and end)}$   
 $v_{y0} =$   
 $v_y =$   
 $a_y = -9.8 \text{ m/s}^2$   
 $t = 5.35 \text{ s}$

B.) Max height?

$$y_{\text{MAX}} = ?$$

$$a_y = -9.8 \text{ m/s}^2$$

$$v_{0y} = \sin(25^\circ) \cdot 62 \text{ m/s}$$

$$v_{0y} = 26.3 \text{ m/s}$$

$$v_y = 0 \text{ m/s}$$

$$v_y^2 = v_{0y}^2 + 2a_y y$$

$$10)^2 = (26.3)^2 + 2(-9.8) \cdot y$$

$$0 = 691.69 - 19.6y$$

$$-691.69 = -19.6y$$

$$y = \frac{-691.69}{-19.6}$$

$$y = 35.3 \text{ m}$$