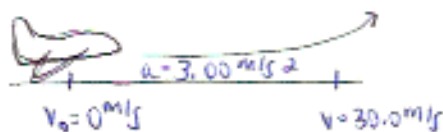


## Kinematics

### Example 5:

A plane is moving down a runway, trying to take off. It begins from rest and must reach a velocity of 30.0 m/s to lift off the ground. The acceleration of the plane is a constant 3.00 m/s<sup>2</sup>. How long must the runway be for the plane to take off?



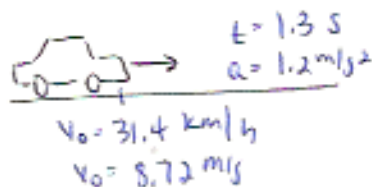
$$\begin{aligned} v_0 &= 0 \text{ m/s} \\ v &= 30.0 \text{ m/s} \\ a &= 3.00 \text{ m/s}^2 \\ x &= ? \end{aligned}$$

$$\begin{aligned} v^2 &= v_0^2 + 2ax \\ (30.0)^2 &= (0)^2 + 2(3.00)x \\ 900 &= 0 + 6x \\ 900 &= 6x \\ x &= \frac{900}{6} \\ \boxed{x = 150 \text{ m}} \end{aligned}$$

### Example 6:

A car has an initial velocity of 31.4 km/h. It accelerates at a uniform rate of 1.2 m/s<sup>2</sup> for 1.3 seconds. Please express your answers in SI units.

- What is the final velocity of the car?
- What is the displacement of the car during this time?



$$\begin{aligned} \text{A.) } t &= 1.3 \text{ s} \\ a &= 1.2 \text{ m/s}^2 \\ v_0 &= 8.72 \text{ m/s} \\ v &= ? \end{aligned}$$

$$\begin{aligned} v &= v_0 + at \\ v &= 8.72 + (1.2)(1.3) \\ v &= 8.72 + 1.56 \end{aligned}$$

$$\boxed{v = 10.3 \text{ m/s}}$$

$$\begin{aligned} \text{B.) } t &= 1.3 \text{ s} \\ a &= 1.2 \text{ m/s}^2 \\ v_0 &= 8.72 \text{ m/s} \\ x &= ? \end{aligned}$$

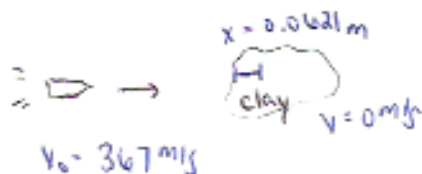
$$\begin{aligned} x &= v_0 t + \frac{1}{2} a t^2 \\ x &= (8.72)(1.3) + \frac{1}{2} (1.2)(1.3)^2 \\ x &= 11.336 + 1.014 \end{aligned}$$

$$\boxed{x = 12.4 \text{ m}}$$

$$\frac{31.4 \text{ km}}{1 \text{ km}} \times \frac{1000 \text{ m}}{1 \text{ km}} \times \frac{1 \text{ h}}{3600 \text{ s}} = 8.72 \text{ m/s}$$

### Example 7:

A bullet is fired from a gun with an initial velocity of 367 m/s before embedding itself into a lump of clay. The bullet penetrates into the clay a distance of 0.0621 m before coming to a stop. Assuming a uniform acceleration, what is the value for the acceleration of the bullet as it moves into the clay?



$$\begin{aligned} v_0 &= 367 \text{ m/s} \\ v &= 0 \text{ m/s} \\ x &= 0.0621 \text{ m} \\ a &= ? \end{aligned}$$

$$\begin{aligned} v^2 &= v_0^2 + 2ax \\ (0)^2 &= (367)^2 + 2a(0.0621) \\ 0 &= 134,689 + 0.1242a \\ -134,689 &= 0.1242a \end{aligned}$$

$$\boxed{a = -1.08 \times 10^6 \text{ m/s}^2}$$