

Getting objects to Rotate



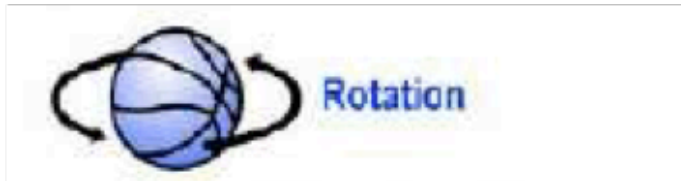
- Net Force is needed to get an object to move



$$F = ma$$

- Net Torque is needed to get an object to rotate

τ



Torque



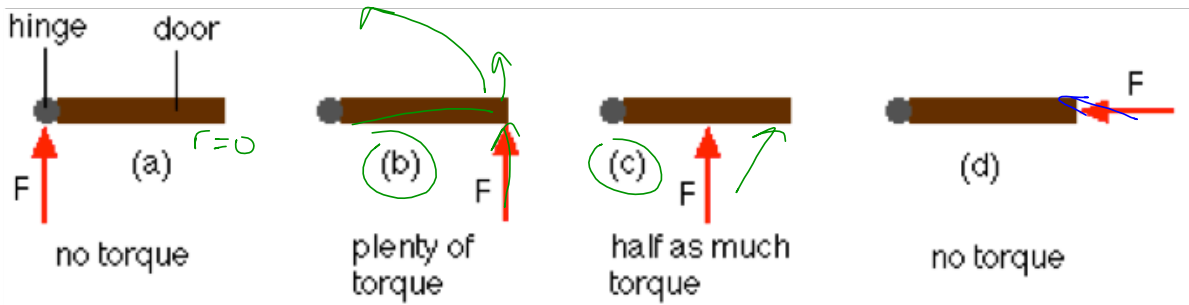
- Newton's second law of rotation

$$F = ma \quad (\text{Forces cause masses to accelerate})$$

$$\tau = r \times F \sin\theta \quad (\text{Torque cause masses to rotate})$$

r ← radius distance from axis of rotation
 \times ← cross product $\begin{bmatrix} 2 & 2 \\ 1 & 0 \end{bmatrix}$
 $\sin\theta$ ← perpendicularly

- Torque are most effective when appliedperpendicularly



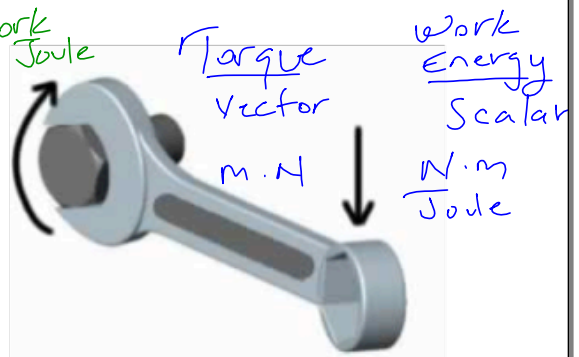
Torque



- Torque (τ) - the ability of a force to turn an object about an axis. 'Turning Power'

- SI Units: Newton meter (m N)

$F \cdot d \rightarrow \text{Work}$
 Joule
 $m \cdot N$
 $\tau = r \times F \sin \theta$



- Vocab:

- Axis of rotation - the point around which the object rotates
- ^(radius) Lever arm - the distance from the axis of rotation to the applied force

Effectiveness of Torque



- Only forces perpendicular to the lever arm will cause any movement. *Or a perpendicular component

$$\tau = r \perp F \longrightarrow \tau = r F \sin \theta$$

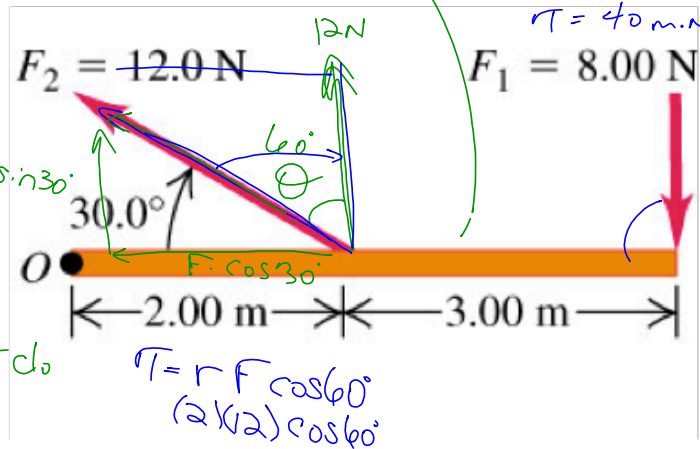
r = distance of lever arm

F = force

$\tau = r \times F \sin \theta$
 $\tau = (5) 8 \sin 90^\circ$
 $\tau = 40 \text{ m}\cdot\text{N}$

- *The θ is the angle needed to give you the perpendicular component

$\tau = r \times F \sin \theta$
 $\tau = (2)(12) \sin 30^\circ$
 $\tau = 12 \text{ m}\cdot\text{N}$
 counter clockwise



Torque Practice



A series of wrenches of different lengths is used on a hexagonal bolt, as shown below. Which combination of wrench length and force applies the greatest torque to the bolt?

a. $T = r F \sin \theta$
 $T = L \cdot F$

b. $T = (L)(2F) \cos 60^\circ$
 $T = L \cdot F$
 $T = r \cdot F \cdot \sin \theta$
 $T = L \cdot (2F) \sin 30^\circ = L \cdot F$

c. $T = r \cdot F \cdot \sin \theta$
 $T = L \cdot 2F \sin 60^\circ$
 $T = L \cdot 2 \cdot F \cdot \frac{\sqrt{3}}{2}$
 $T = \sqrt{3} L \cdot F$
 $T = L \cdot 2F \cdot \cos 30^\circ$

d. $T = r F \cdot \sin \theta$
 $T = \frac{L}{2} (2F)$
 $T = L \cdot F$

Directions for Torque

*By convention

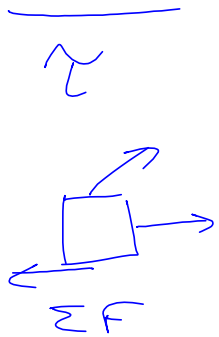
- Positive: Counter-clockwise ◯ Negative: Clockwise



Example 4



Calculate the net torque about the axel of the wheel shown assume that there is a frictional torque of 0.40 Nm that opposes the resulting motion.



$$\sum \tau = \tau_3 - \tau_2 - \tau_1 - (-0.40)$$

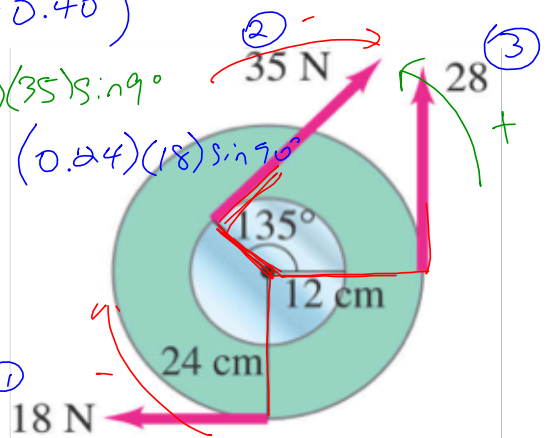
$$\sum \tau = (0.24)(28)\sin 90^\circ - (0.12)(35)\sin 90^\circ - (0.24)(18)\sin 90^\circ$$

$$\sum \tau = 6.72 - 4.2 - 4.32$$

$$\sum \tau = -1.8$$

$$\sum \tau = -1.4 \text{ m}\cdot\text{N}$$

$$\sum \tau = -2.2$$



$$a = -1$$

$$a = -100$$

Example 5



For the wheel-axle system shown, which of the following expresses the condition required for the system to be in static equilibrium?

- A. $m_1 = m_2$
- B. $a m_1 = b m_2$
- C. $a m_2 = b m_1$
- D. $a^2 m_1 = b^2 m_2$
- E. $b^2 m_1 = a^2 m_2$

$$\sum \tau = a \cdot m_1 \cdot g \sin 90^\circ - b m_2 \cdot g \sin 90^\circ$$

$$0 = a m_1 g \sin 90^\circ - b m_2 g \sin 90^\circ$$

$$b m_2 g \sin 90^\circ = a m_1 g \sin 90^\circ$$

$$b m_2 = a m_1$$

F_g is causing torque
 $F_g = mg$

