

Work, Power, & Energy

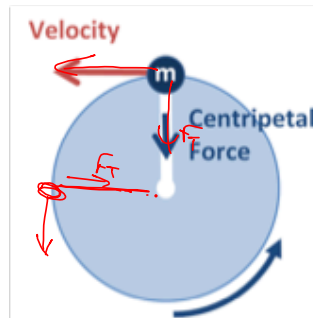
- Work measures the effectiveness of a force
- Also indicates changes in energy

$$\Delta E = W = F_{\parallel} d = F \cdot d \cdot \cos \theta$$

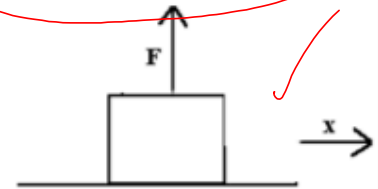
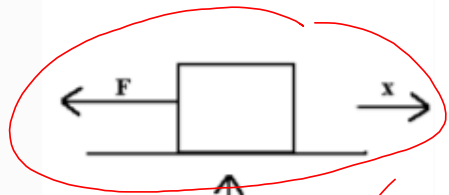
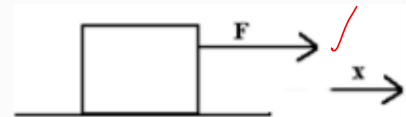
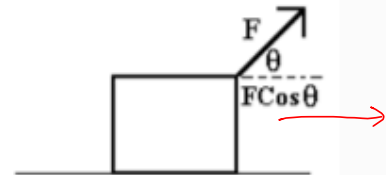
- Measured in Joules

- Positive work = increase of energy
- Negative work = decrease in energy
- 0 Work = no change

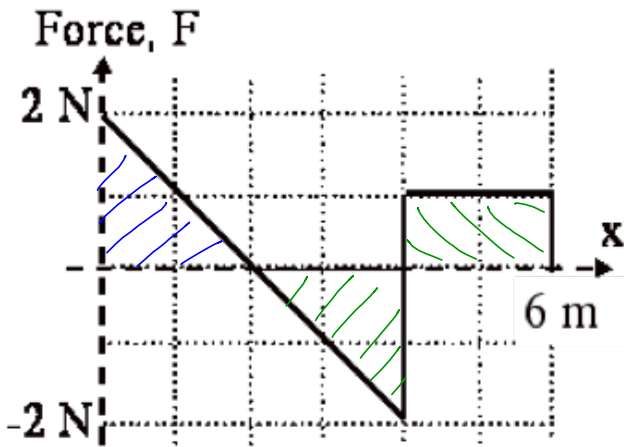
- Centripetal Forces always do 0 work



- Parallel = most effective
- Perpendicular = 0 work



Work, Power, & Energy

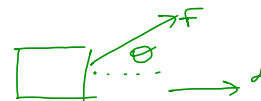


- Graphs – Force vs. Displacement
- Work done by a variable force

$$W = F \cdot d \cdot \cos \theta$$

↳ Assume $\theta = 0^\circ$

W =



- Power = efficiency of a force

- Measured in Watts (W)

$$P = \frac{\Delta E}{t} = \frac{W}{t} = \frac{F \cdot d \cos \theta}{t} = Fv \cos \theta$$

Work, Power, & Energy

- Energy

- Kinetic ($KE = 1/2mv^2$)
- Gravitational Potential ($U = mgh$)
 - Gravitational – Celestial bodies $U_g = \frac{-Gm_1m_2}{r}$
- Elastic Potential ($U_s = 1/2kx^2$)

- Work Energy Theorem

$$\Delta KE = W$$

'Store' energy
 gravity → $U = mgh$
 springs → $U = 1/2kx^2$

'lose' energy

- Conservation of Energy

- Conservative vs Non-Conservative Forces

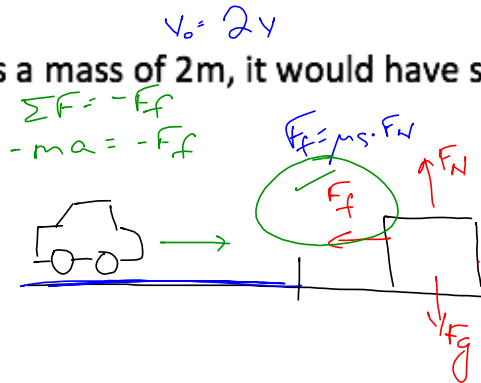
$$\text{Energy}_{\text{end}} = \text{Energy}_{\text{before}} - W_{\text{nc}}$$

Work, Power, & Energy

A car of mass m slides across a patch of ice at a speed v with its brakes locked. It then hits dry pavement and skids to a stop in a distance d . The coefficient of kinetic friction between the tires and the dry road is μ .

If the car has a mass of $2m$, it would have skidded a distance of

- A. $0.5 d$
- B. d**
- C. $1.41 d$
- D. $2 d$



$W = \Delta KE$
 $F \cdot d \cdot \cos\theta = \Delta KE$
 $F_f \cdot d \cdot (-1) = \cancel{\frac{1}{2} m v_f^2} - \frac{1}{2} m v_0^2$
 movement

$\rightarrow F_f \cdot d = -\frac{1}{2} m v_0^2$
 $F_f \cdot d = \frac{1}{2} m v_0^2$
 $m \cdot F_N \cdot d = \frac{1}{2} m v_0^2$
 $\mu \cdot m g \cdot d = \frac{1}{2} m v_0^2$
 $\mu g \cdot d = \frac{1}{2} v_0^2$

Work, Power, & Energy

A car of mass m slides across a patch of ice at a speed v with its brakes locked. It then hits dry pavement and skids to a stop in a distance d . The coefficient of kinetic friction between the tires and the dry road is μ .

If the car has a speed of $2v$, it would have skidded a distance of

- A. d
- B. $1.41 d$
- C. $2 d$
- D. $4 d$

Impulse, Momentum, Collisions

- Momentum – tendency of an object to continue moving after an applied force is removed

$$p = mv \quad \bullet \quad \text{Units } \text{kg} \cdot \frac{\text{m}}{\text{s}}$$

$$v = \frac{2\pi r}{T}$$

- *Linear and angular

- Impulse - All about **how** a force is applied = $F \cdot \Delta t$

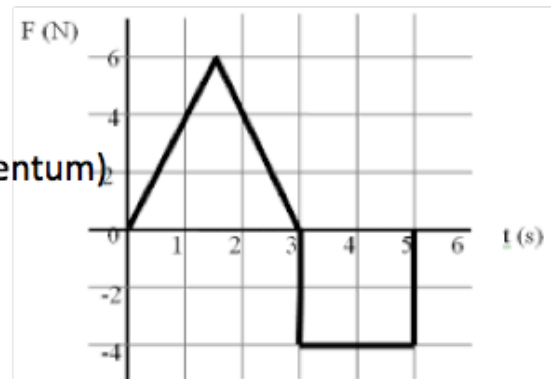
$$F \cdot \Delta t = \Delta p$$

- Impulse required to change an object's momentum

$$\Delta p = F \cdot \Delta t$$

- Area between line & axis of **force vs. time** = Impulse (& change in momentum)

- Impulse & Momentum are both vectors!



Impulse, Momentum, Collisions

- Conservation of momentum (in an isolated system, normally 2 objects)
 - Momentum before interaction = momentum after interaction

$$P_o = P_f$$

- Analyze one dimension at a time

$$* m_1 \cdot v_{1o} + m_2 \cdot v_{2o} = m_1 \cdot v_{1f} + m_2 \cdot v_{2f}$$

- Collisions

- Elastic (perfect physics world)

Momentum Conserved

Yes

KE Conserved

Yes

- Inelastic (realistic physics world)

Yes

No

- ~~*~~ Total Inelastic (things stick together after collision)

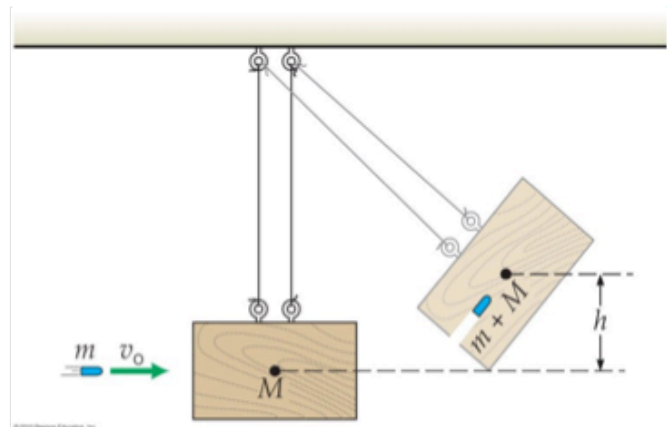
Yes

No

Impulse, Momentum, & Collisions – Ballistic Pendulum

- A ballistic pendulum is a device used to measure the velocities of fast moving projectiles such as bullets. In this example, a 0.0500 kg bullet, initially travelling 150.0 m/s strikes and embeds itself into a wooden ballistic pendulum in a completely inelastic collision. The wood block has a mass of 6.80 kg and was initially at rest.

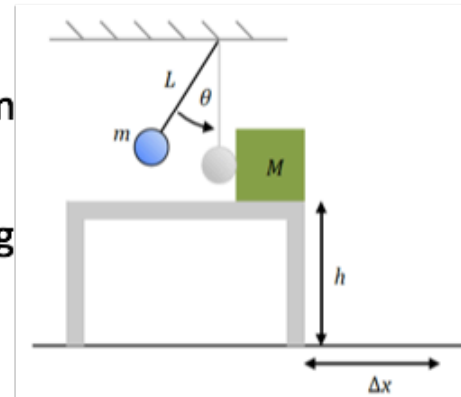
- A. What is the common velocity of the bullet and block after their collision?
- B. Using conservation of energy, find the change in vertical height after the bullet is embedded in the wood?



Impulse, Momentum, & Collisions

Collision + projectile motion

- A pendulum of length $L = 1.0$ meter and bob with mass $m = 1.0$ kg is released from rest at an angle $\theta = 30^\circ$ from the vertical. When the pendulum reaches the vertical position, the bob strikes a mass $M = 3.0$ kg that is resting on a frictionless table that has a height $h = 0.85$ m.



- When the pendulum reaches the vertical position, calculate the speed of the bob just before it strikes the box.
- Calculate the speed of the bob and the box just after they collide elastically.
- Determine the impulse acting on the box during the collision.
- Determine how far away from the bottom edge of the table, Δx , the box will strike the floor.