

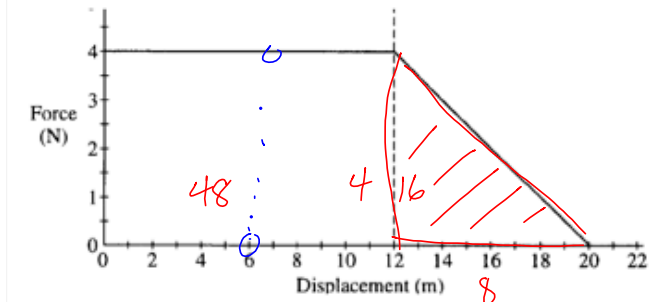
Review



Put in your own words – what is momentum and what is impulse?

What does it mean that momentum is conserved?

Warm-Up



A 0.20 kg object moves along a straight line. The net force acting on the object varies with the object's displacement as shown in the graph above. The object starts from rest at displacement $x = 0$ and time $t = 0$ and is displaced a distance of 20 m. Determine each of the following.

A. The acceleration of the particle when its displacement x is 6 m. $a = ?$

$$F = ma \quad 4 = 0.20 \cdot a \quad a = 20 \text{ m/s}^2$$

B. The time taken for the object to be displaced the first 12 m. $t = ?$

$$x = x_0 + v_0 t + \frac{1}{2} a t^2 \quad x = 12 \text{ m}$$

$$12 = 0 + (0)t + \frac{1}{2}(20)t^2 \quad a = 20 \text{ m/s}^2$$

$$12 = 10t^2 \quad v_0 = 0 \text{ m/s}$$

$$t = 1.10 \text{ s}$$

C. The amount of work done by the net force in displacing the object the first 12 m.

$$W = (4)(12) = 48 \text{ J} \quad F \cdot d$$

$$W = \int \vec{F} \cdot d(\text{cos } \theta)$$

D. The speed of the object at $x = 12$ m.

$$W = \Delta KE \quad 48 = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_0^2$$

$$v = 21.9 \text{ m/s}$$

$$x = 12 \text{ m}$$

$$a = 20 \text{ m/s}^2$$

$$v_0 = 0 \text{ m/s}$$

E. The final speed of the object at displacement $x = 20$ m.

$$W = \Delta KE \quad v = 25.29 \text{ m/s}$$

$$16 = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_0^2$$

$$16 = \frac{1}{2}(0.20)v_f^2 - \frac{1}{2}(0.20)(21.9)^2$$

F. The change in the momentum of the object as it is displaced from $x = 12$ m to $x = 20$ m

$$\Delta p = m v_f - m v_0 = 0.678 \text{ kg} \cdot \text{m/s}$$

$$\Delta p = (0.20)(25.29) - (0.20)(21.9)$$

Example 1



A 0.150 kg baseball moving at +26.0 m/s is brought to rest by a catcher who exerts a constant force of -390.0 N on the ball.

- A. How long does it take to bring the ball to a stop?
- B. Using your kinematic formulas, how far (x) does the ball travel before coming to a stop?

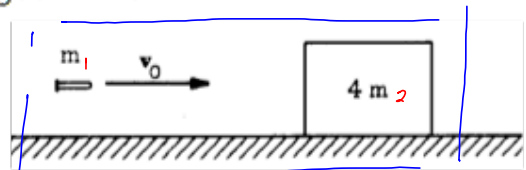
$m = 0.150 \text{ kg}$
 $v_i = 26 \text{ m/s}$
 $v_f = 0 \text{ m/s}$
 $J = \Delta p$
 $F \cdot \Delta t = m v_f - m v_i$
 $\Delta t = 0.01 \text{ s}$

$x = ?$
 $v_0 = 26 \text{ m/s}$
 $v = 0 \text{ m/s}$
 $t = 0.01 \text{ s}$

$v = v_0 + at$
 $x = \frac{1}{2}(v + v_0)t$
 $x = 0.13 \text{ m}$

Example 2

A bullet of mass m and velocity v_0 is fired toward a block of mass $4m$. The block is initially at rest on a frictionless horizontal surface. The bullet penetrates the block and emerges with a velocity of $\frac{1}{3}v_0$.



- A. Determine the final speed of the block.
- B. Determine the loss in kinetic energy of the bullet.

Lost $\frac{4}{9}mv_0^2$

- C. Determine the gain in the kinetic energy of the block.

$KE = \frac{1}{2}mv^2$

$$P_0 = P_f$$

$$m_1 v_{10} + m_2 v_{20} = m_1 v_{1f} + m_2 v_{2f}$$

$$m v_0 + (4m)(0) = m(\frac{1}{3}v_0) + (4m)v$$

$$\frac{3}{3} m v_0 = \frac{1}{3} m v_0 + 4m v$$

$$\frac{2}{3} m v_0 = 4 m v$$

$$\frac{2}{3} v_0 = 4 v$$

$$\frac{1}{6} v_0 = v$$

velocity of block

Before
 $\frac{1}{2} m v_0^2$

After
 $\frac{1}{2} m (\frac{1}{3} v_0)^2$
 $\frac{1}{2} m \frac{1}{9} v_0^2$
 $\frac{1}{18} m v_0^2$

$$\Delta KE = \frac{1}{18} m v_0^2 - \frac{1}{2} m v_0^2$$

$$\Delta KE = \frac{1}{18} m v_0^2 - \frac{9}{18} m v_0^2$$

$$\Delta KE = -\frac{8}{18} m v_0^2$$

$$\Delta KE = -\frac{4}{9} m v_0^2$$



Collisions!!

Three different kinds of collisions

- ▶ **IMPORTANT:** In ALL collisions, momentum is conserved.
 - ▶ Elastic Collisions
 - ▶ Inelastic Collisions
 - ▶ Total Inelastic Collisions

Collisions!

Elastic

'Perfect Physics World'

Perfect Rebound,
no loss of energy

Momentum is
conserved

KE is conserved

$$\frac{1}{2}mv_b^2 = \frac{1}{2}mv_p^2$$

Inelastic

Total Inelastic